Example 7-3: Let y[n] = x[n-10], where x[n] is the sinc function of (??):

$$y[n] = \frac{\sin \hat{\omega}_b(n-10)}{\pi(n-10)}$$

Using the time-delay property and the result for $X(e^{j\hat{\omega}})$ in (??), we can write down the following expression for the DTFT of y[n] with virtually no further analysis:

$$Y(e^{j\hat{\omega}}) = X(e^{j\hat{\omega}})e^{-j\hat{\omega}10} = \begin{cases} e^{-j\hat{\omega}10} & 0 \le |\hat{\omega}| \le \hat{\omega}_b \\ 0 & \hat{\omega}_b < |\hat{\omega}| \le \pi \end{cases}$$

Notice that the magnitude plot of $|Y(e^{j\hat{\omega}})|$ is still a rectangle as in Fig. $\ref{eq:plane}(a)$; time delay only changes the phase in the frequency domain.



McClellan, Schafer, and Yoder, *DSP First*, *2e*, ISBN 0-13-065562-7. Prentice Hall, Upper Saddle River, NJ 07458. ©2016 Pearson Education, Inc.