

**Example 8-1:** In order to compute the 4-point DFT of the sequence  $x[n] = \{1, 1, 0, 0\}$ , we carry out the sum (??) four times, once for each value of  $k = 0, 1, 2, 3$ . When  $N = 4$ , all the exponents in (??) are integer multiples of  $\pi/2$  because  $2\pi/N = \pi/2$ .

$$X[0] = \overset{1}{x[0]}e^{-j0} + \overset{1}{x[1]}e^{-j0} + \overset{0}{x[2]}e^{-j0} + \overset{0}{x[3]}e^{-j0}$$

$$= 1 + 1 + 0 + 0 = 2$$

$$X[1] = 1e^{-j0} + 1e^{-j\pi/2} + 0e^{-j\pi} + 0e^{-j3\pi/2}$$

$$= 1 + (-j) + 0 + 0 = 1 - j = \sqrt{2}e^{-j\pi/4}$$

$$X[2] = 1e^{-j0} + 1e^{-j\pi} + 0e^{-j2\pi} + 0e^{-j3\pi}$$

$$= 1 + (-1) + 0 + 0 = 0$$

$$X[3] = 1e^{-j0} + 1e^{-j3\pi/2} + 0e^{-j3\pi} + 0e^{-j9\pi/2}$$

$$= 1 + (j) + 0 + 0 = 1 + j = \sqrt{2}e^{j\pi/4}$$

Thus, we obtain the four DFT coefficients  $X[k] = \{2, \sqrt{2}e^{-j\pi/4}, 0, \sqrt{2}e^{j\pi/4}\}$ .

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*Note:* The term “coefficient” is commonly applied to DFT values. This is appropriate because  $X[k]$  is the (complex amplitude) coefficient of  $e^{j(2\pi/N)kn}$  in the IDFT (??).

