PROBLEM:

 $h_1[n]$ and $h_2[n]$.

Shown in the figure below is a cascade of two linear time-invariant systems with impulse responses

System #1
$$w[n]$$
 System #2 $h_2[n]$ System #2

The impulse responses of the two systems are

$$h_1[n] = \delta[n] - \frac{1}{2}\delta[n-1]$$
 $h_2[n] = (0.25)^n u[n]$

(a) If
$$x[n] = \delta[n] + \delta[n-1]$$
, find the output of the first system, $w[n]$.

(b) Determine the system function H(z) for the cascade of the two systems. In other words, if y[n] = x[n] * h[n], what is H(z)?

(c) Make a plot of the poles and zeros of
$$H(z)$$
 in the z-plane, where $H(z)$ is the system function found in part (b).

(d) If $x[n] = \delta[n] - (0.25)\delta[n-1]$, find the output of the cascade, y[n].