## PROBLEM:

of the sinusoid:

There are examples on the CD-ROM in the Chapter 3 demos.

(b) For the "chirp" signal

be a positive number?

(a) For the linear-FM "chirp" in (1), determine formulas for the beginning instantaneous frequency  $(\omega_1)$ and the ending instantaneous frequency  $(\omega_2)$  in terms of  $\alpha$ ,  $\beta$  and  $T_2$ . For this problem, assume that the starting time of the "chirp" is t = 0.

A linear-FM "chirp" signal is one that sweeps in frequency from  $\omega_1 = 2\pi f_1$  to  $\omega_2 = 2\pi f_2$  as time goes from t = 0 to  $t = T_2$ . We can define the *instantaneous frequency* of the chirp as the derivative of the phase

 $x(t) = A\cos(\alpha t^2 + \beta t + \phi)$ 

 $x(t) = \Re \left\{ e^{j2\pi (30t^2 - 30t)} \right\}$ 

derive a formula for the instantaneous frequency versus time. Should your answer for the frequency

 $\omega_i(t) = \frac{d}{dt}\psi(t)$  radians/sec

where the cosine function operates on a time-varying argument  $\psi(t) = \alpha t^2 + \beta t + \phi$ The derivative of the argument  $\psi(t)$  is the *instantaneous frequency* which is also the audible frequency heard from the chirp if the chirping frequency does not change too rapidly.

(1)

(2)