PROBLEM:

Consider the following cascade system:

$$\begin{array}{c|c}
x[n] & & LTI \\
System #1 \\
H_1(z) & & H_2(z)
\end{array}$$
LTI System #2 $H_2(z)$

where

$$H_1(z) = 1 - 2z^{-1} + z^{-2}$$
 and $H_2(z) = 1 + z^{-1}$

(a) If the input
$$x[n]$$
 is a step,
$$x[n] = \begin{cases} 1 & \text{for } 0 \le n \\ 0 & \text{for } n < 0 \end{cases}$$

Find the output of the **first filter**, w[n].

(b) Find and plot the impulse response
$$h[n]$$
 of the overall system.