PROBLEM:

Answer the following questions about the time-domain response of FIR digital filters:

$$y[n] = \sum_{k=0}^{M} b_k x[n-k]$$

(a) When tested with an input signal that is an impulse, $x[n] = \delta[n]$, the observed output from the filter is the signal h[n] shown below:

$$\delta[n] = \begin{cases} 1 & \text{for } n = 0 \\ 0 & \text{for } n \neq 0 \end{cases} \longrightarrow \begin{bmatrix} h[n] & 13 & 9 \\ 7 & 9 & 5 & \dots \\ -4 & -1 & 0 & 1 & 2 & 3 & 4 & 5 & n \end{cases}$$

(b) If the filter coefficients are $\{b_k\} = \{13, -13, 13\}$ and the input signal is

Determine the filter coefficients $\{b_k\}$ of the difference equation for the FIR filter.

Determine the inter coefficients $\{b_k\}$ of the difference equation for the FIR inter.

$$x[n] = \begin{cases} 0 & \text{for } n \text{ even} \\ 1 & \text{for } n \text{ odd} \end{cases}$$

determine the output signal y[n] for all n. Give your answer as either a plot or a formula.