PROBLEM:

of the sinusoid:

where the cosine function operates on a time-varying argument $\psi(t) = \alpha t^2 + \beta t + \phi$

(1)

(2)

A linear-FM "chirp" signal is one that sweeps in frequency from $\omega_1 = 2\pi f_1$ to $\omega_2 = 2\pi f_2$ as time goes from t = 0 to $t = T_2$. We can define the *instantaneous frequency* of the chirp as the derivative of the phase

 $x(t) = A\cos(\alpha t^2 + \beta t + \phi)$

The derivative of the argument
$$\psi(t)$$
 is the *instantaneous frequency* which is also the audible frequency heard from the chirp if the chirping frequency does not change too rapidly.

$$\omega_i(t) = \frac{d}{dt}\psi(t)$$
 radians/sec

(a) For the linear-FM "chirp" in (1), determine formulas for the beginning instantaneous frequency
$$(\omega_1)$$
 and the ending instantaneous frequency (ω_2) in terms of α , β and T_2 . For this problem, assume that

the starting time of the "chirp" is
$$t = 0$$
.

range $0 \le t \le 1$ sec.

(b) For the "chirp" signal $x(t) = \Re \left\{ e^{j2\pi(25t^2 - 25t)} \right\}$