PROBLEM:

In this problem you will consider the general case of the "beating" phenomenon. When you multiply two sinusoids:

$$x(t) = \cos(2\pi(40)t - \pi/3)\cos(2\pi(600)t + \pi/4)$$

the signal can still be expressed as a "spectrum." In order to do this, you need an *additive* combination of sinusoids.

- (a) Use the inverse Euler formula to obtain a set of complex exponential signals that sum together to make x(t).
- (b) Plot the spectrum of x(t).
- (c) Find a complex signal z(t) such that $x(t) = \Re e\{z(t)\}$.
- (d) Use the spectrum to write an alternate formula for x(t) as:

$$x(t) = A\cos[2\pi(f_c - \Delta)t + \phi_1] + B\cos[2\pi(f_c + \Delta)t + \phi_2]$$

Find the numerical values for all the parameters: *A*, *B*, f_c , Δ , ϕ_1 , and ϕ_2 .

(e) This signal is periodic; determine its fundamental period.