

PROBLEM:

The system function of a linear time-invariant filter is given by the formula

$$H(z) = (1 - z^{-1})(1 + z^{-2})(1 + z^{-1})$$

- (a) Write the difference equation that gives the relation between the input $x[n]$ and the output $y[n]$.
- (b) What is the output if the input is $x[n] = \delta[n]$?
- (c) Use multiplication of z -transform polynomials to find the output when the input is

$$x[n] = 2\delta[n - 1] + 2\delta[n - 3] - 2\delta[n - 4].$$

- (d) If the input to the system is of the form

$$x[n] = e^{j\hat{\omega}n} \quad -\infty < n < \infty,$$

for what values of $\hat{\omega}$ will the output be zero for all n ? We cannot use z -transforms directly to solve this problem, but we can find the frequency response from $H(z)$ and then solve the problem. Note that the factored form will tell you the answer and so will the pole zero plot for $H(z)$.