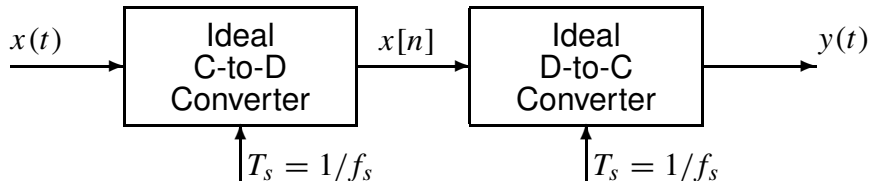


PROBLEM:

We can do some interesting things with sampling. One of them is that we can change the period of a periodic waveform. This problem illustrates how this can be done for the specific periodic input signal

$$x(t) = 2 \cos(2\pi(33)t) + \cos(2\pi(99)t).$$

In all the following parts, assume that the sampling frequency is $f_s = 30$ Hz. Note that this sampling rate *does not* satisfy the conditions of the Shannon sampling theorem, so aliasing will occur.

- Plot the spectrum of the periodic continuous-time signal $x(t)$. What is the fundamental frequency of $x(t)$?
- Determine an expression for the discrete-time signal $x[n]$ as a sum of discrete-time cosine signals. Be sure that all of the normalized frequencies are positive and less than π radians. Plot the spectrum of $x[n]$ over the range of normalized frequencies $-\pi \leq \hat{\omega} \leq \pi$.
- Now the continuous-time output signal $y(t)$ that is created by the ideal D-to-C converter operating with sampling rate $f_s = 30$ Hz will also be a sum of cosine signals. Write an expression for $y(t)$ and plot its spectrum. What is the fundamental frequency of $y(t)$?
- How are the fundamental frequencies of $x(t)$ and $y(t)$ related? Do you think that it would be possible to change the fundamental frequency by a different factor by using a different sampling rate?