PROBLEM:

We now have four ways of describing an LTI system: the difference equation; the impulse response, h[n]; the frequency response, $H(e^{j\hat{\omega}})$; and the system function, H(z). In the following, you are given one of these representations and you must find the other three.

(a)
$$y[n] = (x[n] + 2x[n-2] + x[n-4]).$$

(b)
$$h[n] = \delta[n] + \delta[n-1] + \delta[n-2] + \delta[n-3] + \delta[n-4].$$

(c) $H(e^{j\hat{\omega}}) = [1 + \cos(2\hat{\omega})]e^{-j\hat{\omega}^3}$. *Hint: Expand the cosine using Euler's formula.*

(d)
$$H(z) = 1 - 2z^{-2} + z^{-4} + z^{-7}$$
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