

PROBLEM:

The diagram in Figure 1 depicts a *cascade connection* of two linear time-invariant systems; i.e., the output of the first system is the input to the second system, and the overall output is the output of the second system.

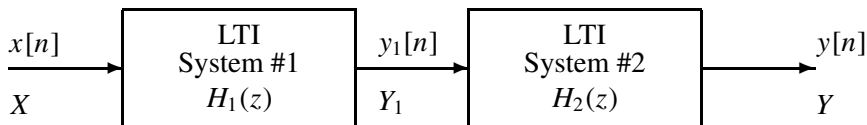


Figure 1: Cascade connection of two LTI systems.

- Use z -transforms to show that the system function for the overall system (from $x[n]$ to $y[n]$) is $H(z) = H_2(z)H_1(z)$, where $Y = H(z)X$.
- Derive a condition on $H(z)$ that guarantees that the output signal will always be equal to the input signal.
- Suppose that System #1 is an FIR filter described by the difference equation $y_1[n] = x[n] + \frac{5}{6}x[n-1]$ and System #2 is described by the system function $H_2(z) = 1 - 2z^{-1} + z^{-2}$. Determine the system function of the overall cascade system.
- Obtain a single difference equation that relates $y[n]$ to $x[n]$ in Figure 1.
- Plot the poles and zeros of $H(z)$ in the complex z -plane.
- If System #1 is the difference equation: $y_1[n] = x[n] + \frac{5}{6}x[n-1]$, find a system function $H_2(z)$ so that output of the cascaded system will always be equal to its input. In other words, find $H_2(z)$ which will undo the filtering action of $H_1(z)$. This is called *deconvolution*.