PROBLEM:

A chirp signal is synthesized according to the following formula:

$$x(t) = \Re e\{e^{j2\pi}(500t^2 + 700t + 900)\} \qquad \text{for } 0 \le t \le 3$$

(a) Derive the sinusoidal formula for x(t).

(b) Determine the formula for the instantaneous frequency of the chirp.

(c) Make a plot of the instantaneous frequency versus time.

(d) Derive a formula similar to x(t) for a chirp signal whose instantaneous frequency starts at 7 kHz and falls linearly to 3 kHz in 3 seconds.