PROBLEM:

In the following cascade of systems, all systems are defined by their transfer functions.

$$H_{1}(z) \xrightarrow{v_{1}[n]} H_{2}(z) \xrightarrow{v_{2}[n]} H_{3}(z) \xrightarrow{y[n]} H_{3}(z)$$

$$H_{1}(z) = \frac{5}{1 - \frac{1}{2}z^{-1}} \qquad H_{2}(z) = 4z^{-1} - z^{-2} \qquad H_{3}(z) = \frac{\beta_{0} + \beta_{1}z^{-1}}{1 + \alpha z^{-1}}$$

1]). Determine the overall system function H(z) which is a unit-delay. Then state how H(z) is related to $H_1(z)$, $H_2(z)$ and $H_3(z)$.

(a) Suppose that the cascade of the three systems is equivalent to a unit-delay system (i.e., y[n] = x[n -

(b) Determine the unknown coefficients of $H_3(z)$, so that the overall system will be a unit-delay system. Find numerical values for $\{\beta_0, \beta_1, \alpha\}$.