PROBLEM:

A linear time-invariant system is described by the difference equation

$$y[n] = x[n] - \beta x[n-1]$$

(a) When the input to this system is

$$x[n] = \begin{cases} 0 & n < 0\\ \beta^n & n = 0, 1, 2, 3, 4, 5\\ 0 & n > 5 \end{cases}$$

Use convolution to compute the values of y[n], over the range $0 \le n \le 6$. Give a general formula in terms of β , and also show that most of the output values are equal to zero.

(b) Use the results from the previous part and plot both x[n] and y[n] for the case where $\beta = \frac{1}{2}$.