PROBLEM:

frequency

 $C^{\overline{\#}}$ $F^{\#}$ E^{\flat} R^{\flat} Cnote name D 40 42 43 44 45 47 52 note number 41 46 48 49 50 51

We have seen that musical tones can be modeled mathematically by sinusoidal signals. If you read music or play the piano you are aware of the fact that the piano keyboard is divided into octaves, with the tones in each octave being twice the frequency of the corresponding tones in the next lower octave. To calibrate the frequency scale, the reference tone is the A above middle-C, which is usually called A440 since its frequency is 440 Hz. Each octave contains 12 tones, and the ratio between the frequencies of successive tones is constant. Since middle C is 9 tones below A440, its frequency is approximately $(440)2^{-9/12} \approx 262$ Hz. The names of the tones (notes) of the octave starting with middle-C and ending with high-C are:

/ \	т 1 .	1 4	1 .	C 41		C	• ,	es must be $2^{1/12}$.
(2)	Hynlain	why f	the ratio	Of the	treamencie	e ot	SUCCESSIVE NOT	e milet he 71/12
(a)	LAPIGIII	WILLY U	me rano	or uic	11 Cquciicic	3 01	successive non	o musi oc 2 .

(b)	Make a table of the frequencies of the tones of the octave beginning with middle-C assuming that A
	above middle C (note #49) is tuned to 440 Hz.

the frequency of the corresponding tone, give a formula for the frequency of the tone as a function of the note number.

(c) The above notes on a piano are numbered 40 through 52. If n denotes the note number, and f denotes

(d) A *chord* is a combination of musical notes sounded simultaneously. A *triad* is a three note chord.

The C Minor chord is composed of the tones of C E^{\flat} G sounded simultaneously. From the set of corresponding frequencies determined in part (a), make a sketch of the essential features of the spectrum of the C Minor chord assuming that each note is realized by a pure sinusoidal tone and that

each note is equally loud. (You do not have to specify the complex amplitudes precisely.)