## PROBLEM:

of the sinusoid:

 $\psi(t) = \alpha t^2 + \beta t + \phi$ 

A linear-FM "chirp" signal is one that sweeps in frequency from  $\omega_1 = 2\pi f_1$  to  $\omega_2 = 2\pi f_2$  as time goes from t = 0 to  $t = T_2$ . We can define the *instantaneous frequency* of the chirp as the derivative of the phase

 $x(t) = A\cos(\alpha t^2 + \beta t + \phi)$ 

The derivative of the argument  $\psi(t)$  is the *instantaneous frequency* which is also the audible frequency heard

$$\psi(\iota) = \alpha \iota + \rho \iota +$$

where the cosine function operates on a time-varying argument

 $\omega_i(t) = \frac{d}{dt}\psi(t)$  radians/sec

from the chirp if the chirping frequency does not change too rapidly.

There are examples on the CD-ROM in the Chapter 3 demos. (a) For the linear-FM "chirp" in (1), determine formulas for the beginning instantaneous frequency ( $\omega_1$ )

and the ending instantaneous frequency  $(\omega_2)$  in terms of  $\alpha$ ,  $\beta$  and  $T_2$ . For this problem, assume that the starting time of the "chirp" is t = 0. (b) For the "chirp" signal

range  $0 \le t \le 1$  sec.

derive a formula for the instantaneous frequency versus time.

(c) For the signal in part (b), make a plot of the *instantaneous* frequency (in Hz) versus time over the

(1)

(2)

$$x(t) = \Re \left\{ e^{j2\pi(-33t^2 + 98t - 0.2)} \right\}$$