PROBLEM:

the first system is the input to the second system, and the overall output is the output of the second system.

The diagram in Fig. 1 depicts a cascade connection of two linear time-invariant systems; i.e., the output of

$$\begin{array}{c|c} x[n] & \text{LTI} \\ \text{System #1} \\ \mathcal{H}_1(\hat{\omega}) & y_1[n] \\ \end{array} \begin{array}{c} \text{LTI} \\ \text{System #2} \\ \mathcal{H}_2(\hat{\omega}) \\ \end{array}$$
 Figure 1: Cascade connection of two LTI systems.

(a) Suppose that System #1 is described by the difference equation $y_1[n] = x[n] + x[n-2]$. and System

#2 is described by the frequency response function
$$\mathcal{H}_2(\hat{\omega}) = (1 - e^{-j2\hat{\omega}})$$
. Determine the frequency response function of the overall cascade system.

(b) Obtain a single difference equation that relates y[n] to x[n] in Fig. 1.